

Intrinsic Ferroelectric Switching in Two-Dimensional α -In₂Se₃

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Cite This: ACS Nano 2024, 18, 26103–26114



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ABSTRACT: Two-dimensional (2D) ferroelectric semiconductors present opportunities for integrating ferroelectrics into high-density ultrathin nanoelectronics. Among the few synthesized 2D ferroelectrics, α -In₂Se₃, known for its electrically addressable vertical polarization, has attracted significant interest. However, the understanding of many fundamental characteristics of this material, such as the existence of spontaneous in-plane polarization and switching mechanisms, remains controversial, marked by conflicting experimental and theoretical results. Here, our combined experimental characterizations with piezoresponse force microscope and symmetry analysis conclusively dismiss previous claims of in-plane ferroelectricity in single-domain α -In₂Se₃. The processes of vertical polarization switching in monolayer α -In₂Se₃ are explored with deep-learning-assisted large-scale molecular dynamics



simulations, revealing atomistic mechanisms fundamentally different from those of bulk ferroelectrics. Despite lacking inplane effective polarization, 1D domain walls can be moved by both out-of-plane and in-plane fields, exhibiting avalanche dynamics characterized by abrupt, intermittent moving patterns. The propagating velocity at various temperatures, field orientations, and strengths can be statistically described with a universal creep equation, featuring a dynamical exponent of 2 that is distinct from all known values for elastic interfaces moving in disordered media. This work rectifies a long-held misunderstanding regarding the in-plane ferroelectricity of α -In₂Se₃, and the quantitative characterizations of domain wall velocity will hold broad implications for both the fundamental understanding and technological applications of 2D ferroelectrics.

KEYWORDS: 2D ferroelectrics, α -In₂Se₃, domain wall dynamics, in-plane polarization, deep potential molecular dynamics

INTRODUCTION

For a ferroelectric thin film, the depolarization field that arises due to the imperfect screening of polarization bound charges on surfaces is inversely proportional to the thickness of the film.1 The suppressed polarization along the direction of reduced dimensionality has been a main obstacle for the miniaturization of ferroelectric-based devices. Among the limited number of synthesized two-dimensional (2D) ferroelectrics, α -In₂Se₃ has garnered considerable attention, mainly because of its advantageous out-of-plane polarization (P_{OP}) in the monolayer limit.²⁻⁴ This characteristic allows for full utilization of the atomic thickness for the development of highperformance, ultrathin nanoelectronics.⁵ Notably, the 2D ferroelectricity in α -In₂Se₃ was first predicted theoretically based on density functional theory (DFT) calculations,² which was later confirmed experimentally.^{3,4} Several device prototypes, including ferroelectric channel transistor⁶ and synaptic ferroelectric semiconductor junction,⁷ have been fabricated using quasi-2D In₂Se₃ films with a thickness of tens of nanometers. In addition to forming the α phase, In₂Se₃ can

crystallize into the β' phase with in-plane polarization ($P_{\rm IP}$) and the paraelectric β phase (Figure 1a).^{8–11} Leveraging both polymorphism and ferroelectricity of In₂Se₃ establishes a versatile platform for device design.¹²

Recent experiments have demonstrated that van der Waals (vdW) stacked bilayers of nonferroelectric monolayers can be engineered into ferroelectrics through sliding and twisting, $^{13-17}$ thus substantially expanding the family of 2D ferroelectrics possessing $P_{\rm OP}$. Much like their bulk counterparts, the functional attributes of 2D ferroelectrics depend critically on the polarization response to external stimuli, whereas it is not clear whether various switching models developed for bulk ferroelectrics can be directly applied to

Received:May 19, 2024Revised:August 31, 2024Accepted:September 6, 2024Published:September 16, 2024







Figure 1. OP- and IP-PFM measurements on α -In₂Se₃using AFM probes with different force constants. Schematics of (a) paraelectric β phase and (b) ferroelectric α phase with Wyckoff positions (WPs) labeled. For simplicity, the top view of α -In₂Se₃ does not display the outermost Se atoms. The table presents the splitting rules of WPs for the phase transition of $P\overline{3}m1 \rightarrow P3m1$. The In atoms in α -In₂Se₃ occupy 1a and 1c orbit, respectively, which does not confirm to the 2d \rightarrow 1b/1c splitting rule for the symmetry break $P\overline{3}m1 \rightarrow P3m1$. (c) Vertical and lateral surface tuning spectra using a probe with (c) $k \approx 2.8$ N/m and (e) $k \approx 0.2$ N/m. (d) AFM topographic image of the measured α -In₂Se₃ flake. (f) OP- and IP-PFM amplitude and phase images acquired by the probe with (f) $k \approx 2.8$ N/m and (g) $k \approx 0.2$ N/m.

reduced dimensions.¹⁸ At the most fundamental level, the controlled engineering of ferroelectric switching in 2D hinges on a quantitative characterization of the dynamics of 1D domain walls, which are nanoscale interfaces between differently polarized 2D domains. This endeavor has been particularly challenging due to the high temporal and spatial resolution required for both experimental and theoretical approaches, such that there is virtually no reported data on the velocity of 1D domain walls in 2D ferroelectrics. In this work, we use 2D α -In₂Se₃ as a model system to investigate the switching mechanisms in 2D.

The structural origin of P_{OP} in monolayer α -In₂Se₃ (space group P3m1) is unambiguous: it results from the shift of the

central Se layer along the *z*-axis that breaks the out-of-plane inversion symmetry (Figure 1b). Despite extensive studies, several specifics of ferroelectricity in 2D α -In₂Se₃ remain unclear. Particularly, there is an ongoing debate regarding whether monolayer α -In₂Se₃ exhibits electrically switchable inplane effective polarization ($P_{\rm IP}$). In the original paper predicting 2D ferroelectricity in monolayer α -In₂Se₃,¹⁹ it was argued that it should also possess $P_{\rm IP}$, mainly deduced from the cross-sectional crystal structure which suggests a lateral offcentered displacement of Se atom. However, as pointed out by follow-up studies,²⁰ the C_{3v} point group symmetry (out-ofplane 3-fold rotational axis) of α -In₂Se₃ strictly prohibits inplane switchable polarization (also refereed to as *effective* polarization in modern theory of polarization^{21,22}), according to Neumann's principle. This is evident from the top view of α -In₂Se₃, similar to *h*-BN (Figure S1), which is invariant with respect to a 3-fold rotation thus nullifying any in-plane spontaneous polarization. Nevertheless, multiple experimental studies have reported switching-like behaviors when in-plane electric fields ($\epsilon_{\rm IP}$) are applied to α -In₂Se₃ thin films.^{23,24}

Another experiment-theory conundrum for 2D α -In₂Se₃ involves the coercive field that switches $P_{\rm OP}$. Previous DFT investigations have indicated a rather low switching barrier of ≈ 66 meV per unit cell (uc) in monolayer α -In₂Se₃,¹⁹ yet the observed out-of-plane switching field is commonly above 1 V/ nm $(10 \text{ MV/cm})^4$ several orders of magnitude higher than that for PbTiO₃-based perovskite ferroelectrics ($\approx 10 \text{ kV}/$ cm)²⁵ which actually have larger switching barriers (\approx 200 meV/uc). The low barrier predicted by DFT does not support "dipole locking mechanism", which proposes that the locked out-of-plane and in-plane motion of the middle Se atom would lead to a large barrier.⁴ We note that this terminology has its own issues, as it could be mistakenly interpreted as the locking between out-of-plane and in-plane net dipoles, despite the original work explicitly stating that there is only in-plane asymmetry (see additional discussions in Supplementary Section I). This asymmetry does not lead to in-plane net electric dipole (due to 3-fold rotational symmetry), but it allows for effective in-plane second-order optical dipole emission. Such experiment-theory conundrum appears to be a common feature for vdW bilayers exhibiting sliding ferroelectricity. For example, the DFT-predicted switching barrier for Bernal-stacked h-BN possessing sliding ferroelectricity is only 8 meV/uc,²⁶ yet the experimental switching field is on the order of 0.1 V/nm. 13,22

To summarize, currently there is no consensus, be it experimental or theoretical, on several key questions: (i) Does monolayer α -In₂Se₃ exhibit switchable $P_{\rm IP}$? (ii) Why does 2D α -In₂Se₃, similar to vdW bilayers of stacking-engineered ferroelectricity, exhibit such a high out-of-plane switching field? (iii) What are the polarization switching dynamics involved in 2D domains and 1D walls? Here, we address these questions with both experimental characterizations and a multiscale modeling approach that combines symmetry analysis, DFT calculations, and deep-learning-assisted large-scale molecular dynamics (MD) simulations.

RESULTS AND DISCUSSION

Symmetry Analysis of \alpha-ln₂Se₃. Monolayer α -ln₂Se₃ is in the space group of P3m1, while the bulk forms adopting 3R and 2H stacking orders are in the space groups of $P6_{3}mc$ and R3m, respectively. All these space groups exhibit a 3-fold rotational axis along z (the out-of-plane direction for the monolayer). Proper symmetry analysis should lead to a straightforward conclusion: there is only in-plane piezo-electricity due to the in-plane inversion symmetry breaking, but there is no in-plane ferroelectricity. The in-plane asymmetry of α -ln₂Se₃ is similar to that in 2H or 3R MoS₂ and *h*-BN. It is possible that residual uniaxial strains in α -ln₂Se₃ samples could disrupt the 3-fold rotational symmetry, and the piezoelectric effect gives rise to finite but nonreversible P_{IP} .

The resilience of P_{OP} against the depolarization field in 2D α -In₂Se₃ can also be understood with a symmetry argument, viewing the switching process from the ferroelectric to the reference paraelectric phase as an electric field-driven phase transition. The Landau theory of group-subgroup structural

phase transitions presumes that transitions result from the condensation of either a single or a group of collective degrees of freedom, conforming to a single irreducible representation (irrep) of the space group for the high-symmetry phase. Within a space group, atoms occupy specific positions known as Wyckoff positions (or orbits), defined by their symmetry properties within the space group. Wyckoff orbit splitting refers to the phenomenon where a set of equivalent atomic positions in a crystal becomes distinct and nonequivalent due to a reduction in symmetry during a group-subgroup phase transition. Each type of group-subgroup transition has its own set of restrictions on how these splittings can occur (see the example of the paraelectric-ferroelectric phase transition of PbTiO₃ in Figure S2). We find that though paraelectric β - In_2Se_3 (space group P3m1) and ferroelectric α -In₂Se₃ (space group P3m1) conform to the group-subgroup relationship, the $\beta \leftrightarrow \alpha$ transition cannot be realized by a structural distortion associated with an irrep of $P\overline{3}m1$, because the atomic occupations in β -In₂Se₃ and α -In₂Se₃ do not conform to the required splitting of Wyckoff positions. Specifically, the In atoms occupy the 2d Wyckoff orbits in β -In₂Se₃, while the two In atoms in α -In₂Se₃ occupy 1a and 1c orbit, respectively, violating the allowed splitting rule of $2d \rightarrow 1b/1c$ associated with $P3m1 \rightarrow P3m1$ (see Figure 1a,b). This is fundamentally different from (proper) perovskite ferroelectrics, where a polar soft mode identified by an irrep serves as the primary order parameter responsible for the paraelectric-ferroelectric phase transition.²⁸ Given that a depolarization field mainly suppresses the displacive distortion associated with the polar soft mode, we propose that P_{OP} in 2D α -In₂Se₃ is protected by a principle we call "splitting restriction", which refers to the forbidden splitting of Wyckoff orbits during the postulated phase transition. We highlight that the same mechanism also plays a role in the stabilization of P_{OP} emerged in sliding and moiré ferroelectricity²⁹⁻³² (see detailed discussions about Bernalstacked *h*-BN in Supplementary Section VII). Additionally, the splitting restriction principle predicts that $\beta \rightarrow \beta'$ could be favored over $\beta \rightarrow \alpha$, which is consistent with our Raman spectroscopy characterizations of $2H-\alpha$ -In₂Se₃ during a heating-cooling cycle (see Supplementary Section II).

Piezoelectric Response Microscopy Characterizations of α -ln₂Se₃. The aforementioned symmetry analysis resoundingly indicates the absence of switchable $P_{\rm IP}$ in α -In₂Se₃, contrasting to a flurry of research studies that have claimed its existence. Nearly all reports of the presence of $P_{\rm IP}$ in 2D α -In₂Se₃ depended on measurements of piezoresponse force microscopy (PFM) with the Dual AC Resonance Tracking (DART) mode.^{3,23,24,33-35} We will first argue, based on fundamental PFM theory, that acquiring in-plane PFM (IP-PFM) signal in α -In₂Se₃ is not possible. In IP-PFM studies, the piezoresponse signal is related to the torsional motion of the atomic force microscopy (AFM) probe, which is caused by the shear strain of the sample under vertical electric field. The relevant piezoelectric coefficient in this process is d_{35} (or d_{34}), where the subscript 5 (or 4) denotes the induced shear strain in xz (or yz) plane under Voigt notation (Figure S4). However, for monolayer α -In₂Se₃ with a space group P3m1, both d_{35} and d_{34} components are zero within its piezoelectric tensorial matrix. The same situation applies to bulk α -In₂Se₃ with 2H or 3R stacking order (Figure S5). It is worth noting that the symmetric distribution of the IP electric field component of the AFM probe in conjunction with the 3-fold



Figure 2. Comparative study by angle-resolved IP-PFM. Angle-resolved IP-PFM images of (a) α -In₂Se₃ and (b) NbOI₂. The polar plots in the center of (a) and (b) are the extracted mean amplitude of each PFM image at respective azimuthal angle. The measurement conditions were fixed for two samples.

rotational symmetry also prohibits the detection of nonzero IP piezoelectric tensor elements (e.g., d_{22}).

Second, it is well-known in the PFM community that out-ofplane and in-plane deformation signals are strongly convoluted in practical measurements.^{36,37} Thus, special care and a proper measurement protocol are required to unambiguously separate the vertical and lateral contributions with correct interpretations of the results, which were seriously lacking in previous studies of α -In₂Se₃ (see case-by-case analysis of the previous reports in Supplementary Section III). Herein, we perform a comparative PFM study on α -In₂Se₃ thin flakes exfoliated onto highly doped silicon substrate (Figure 1d) by using two AFM probes with different force constants. One probe has a force constant (k) of ≈ 2.8 N/m, similar to those widely used in previous reports, while the other is much softer ($k \approx 0.2 \text{ N/m}$) with better torsional sensitivity.³⁸ Both the out-of-plane and inplane surface tuning spectra for both probes were recorded first to determine the contact resonance between the probe and the sample for the subsequent DART PFM measurements. As shown in Figure 1c,e, the resonant peaks for vertical deflection and lateral torsion modes are distinct from each other for both probes. The α -In₂Se₃ sample used here contains mixed 2H and 3R stacking, as confirmed by our Raman and SHG measurements (Figure S7). Similar incommensurate stacking structure is commonly observed in chemical vapor-grown In₂Se₃ single crystals.^{39,40} Such sample, however, helps us exclude the existence of P_{IP} in both stacking types as detailed below.

Next, OP- and IP-PFM images are acquired using both probes driven by an AC voltage at their respective first harmonic frequencies. A box-in-box pattern was written by a DC biased probe in advance, as a reference for the following measurements. For OP-PFM, both probes provide strong piezoresponse amplitude on the α -In₂Se₃ surface compared with the Si substrate. Additionally, the phase images show sharp 180° difference between upward and downward domains, confirming the noticeable piezoresponse (d_{33}) in the out-of-plane direction. For IP-PFM, however, although we observe sizable "amplitude signal", it is not distinguishable between α -In₂Se₃ and the nonpiezoelectric Si substrate. As mentioned, this spurious signal originates from the electronic background of the lock-in amplifier at high frequency. The phase image obtained by the stiff probe exhibits a domain pattern identical to the OP-PFM image (Figure 1f), yet the phase difference between oppositely polarized domains is much less than 180° . Thus, the observed IP piezoresponse signal is probably a crosstalk effect from the OP signal.^{36,37} By using a soft probe, this effect is reduced, but still visible (Figure 1g).

Another important practice in PFM to confirm the intrinsic in-plane response is to perform an angular-resolved lateral PFM by rotating the sample at different azimuthal angles with regard to the AFM cantilever.^{38,41} We carry out a comparative study by conducting angle-resolved IP-PFM on both 2H α -In₂Se₃ and NbOI₂ with known in-plane ferroelectricity under the same measurement condition, with the results summarized in Figure 2. The measured IP-PFM amplitude is maximized when the direction of $P_{\rm IP}$ is perpendicular to the cantilever axis and minimized when they are parallel to each other. Hence, we should expect the IP-PFM amplitude to follow an absolute sinusoidal function with a period of 180°. This is exactly what is observed in the central polar plot of Figure 2b for NbOI₂, and the in-phase signal also changes its sign (phase reversal) when the sample is rotated by 180°. In stark contrast, the α -In₂Se₃ sample with a prewritten box-in-box pattern shows no periodic modulation in both IP-PFM amplitude and phase (Figure 2a), suggesting the measured lateral response does not originate from intrinsic in-plane piezoresponse. Given the above symmetry analysis and experimental results, we can safely exclude the existence of $P_{\rm IP}$ in both 2H and 3R α -In₂Se₃.

The out-of-plane piezoresponse and polarization, on the contrary, is confirmed (Figure 1) in our PFM investigations. We note that the out-of-plane switching field is extremely large, consistent with the prediction of splitting restriction principle. In an upward domain of a 30 nm-thick flake on highly doped Si, it is only possible to obtain a minor hysteresis loop (incomplete switching) under a DC voltage up to 9 V (Figure S8d), while no sign of switching is observed in the downward domain (Figure S8e). At such a high field, irreversible surface modification due to the electrochemical process starts to take place (Figure S8a). The results indicate that the out-of-plane



Figure 3. Domain switching in monolayer α -In₂Se₃. (a) Minimum energy paths of polarization reversal identified with DFT-based NEB for various ε_{OP} magnitudes. The inset illustrates primary atomic movement patterns during this low-barrier switching pathway: entire layers of In and Se atoms need to move laterally in the same direction. This pathway is the same as the one reported in ref 19. (b) Analytical nucleation energy (ΔU_{nuc}) computed with DFT and MD parameters as a function of nucleus size (N) across various strengths of ε_{OP} .

coercive field is possibly beyond 3 MV/cm. For comparison, vdW ferroelectric CuInP₂S₆ with a similar thickness shows a coercive field below 1 MV/cm under the same measurement condition (Figure S8f). Interestingly, we find that the switching field is greatly reduced when the biased AFM probe is scanning on the sample surface, which could explain the widely reported domain switching behaviors in the literature. As detailed by our theoretical calculations below, it is indeed much easier to drive polarization switching through domain wall motions with an in-plane electric field despite the lack of in-plane ferroelectricity in monolayer α -In₂Se₃.

Domain Switching in 2D α **-In**₂Se₃. We now address the second experiment-theory conundrum: why experimentally a large out-of-plane electric field (ε_{OP}) is required to switch α -In₂Se₃, despite the identification of a low-barrier pathway using the DFT-based nudged elastic band (NEB) technique. By carefully designing a pathway that connects the upward polarized and downward polarized monolayer α -In₂Se₃, Ding etal obtained a NEB barrier (ΔU^{NEB}) of 66 meV/uc.¹⁹ Our calculated value for the same pathway is 40 meV/uc (Figure 3a), due to the usage of more intermediate images and tighter convergence threshold. However, a critical issue with NEB is that this method requires the manual construction of an initial pathway, which can potentially be subject to human bias, and there is no guarantee that such a manually designed pathway can be physically activated by $\varepsilon_{\mathrm{OP}}$. Indeed, we find that this low-barrier pathway involves concerted lateral shifts of entire layers of In and Se atoms (see inset of Figure 3a), coupled with out-of-plane displacements that reverse P_{OP} . We suggest that it is highly improbable for ε_{OP} to activate this process: In and Se atoms, bearing opposite charges, should move in opposite directions under the influence of $\varepsilon_{\mathrm{OP}}$, rather than moving in the same direction as assumed in NEB calculations. We further perform finite-field NEB calculations with varying ε_{OP} magnitudes and confirm that ΔU^{NEB} is weakly dependent on field strength: even an intense ε_{OP} of 3.0 V/nm (30 MV/cm) only moderately reduces the barrier (Figure 3a). This corroborates with the splitting restriction principle that suggests the absence of a symmetry-adapted polar mode for efficient $P_{\rm OP} - \varepsilon_{\rm OP}$ coupling.

Another aspect is that ΔU^{NEB} corresponds to the barrier for a homogeneous switching mechanism during which all dipoles response synchronously to ε_{OP} without nucleating oppositely polarized domains. This overlooks the energy costs involved in creating interfaces that separate the newly formed nucleus and the surrounding domain. The difficulty of reversing P_{OP} in an ideal 2D domain of α -In₂Se₃ via ε_{OP} is further corroborated by our large-scale MD simulations that employs a deep neural network-based force field trained with a large database of ab initio energies and atomic forces from ≈25,000 configurations of $In_2Se_3^{42}$ (see Methods). We observe that a single-domain monolayer, constructed using an 18,000-atom supercell, is immune to $\varepsilon_{\rm OP}$ at 300 K (no switching detected within a simulation period of 3 ns), even when exposed to giant field strengths achievable in experimental setups. Only at an elevated temperature of 373 K is a nucleus formed with P_{OP} aligned with ε_{OP} of 3.0 V/nm (Figure S13). The change in the energy associated with the formation of a 2D nucleus containing N unit cells can be approximated as⁴³

$$\Delta U_{\rm nuc} = -2N\mathcal{E}_{\rm OP}p_{\mu} + g\sqrt{N}\sigma_i \tag{1}$$

where p_{μ} is the out-of-plane electric dipole moment per unit cell, σ_i is the (averaged) interface energy per unit-cell length of the boundary that separates the nucleus and the parent domain, and g is a geometric factor depending on the nucleus shape. Detailed derivations for eq 1 are provided in Supplementary Section VIII. Using $p_u = 0.09 \text{ eÅ}$ computed with DFT, $\sigma_i = 0.23$ eV and $g = 8/\sqrt{3}$ both extracted from MD, Figure 3b displays $\Delta U_{\rm nuc}$ as a function of N for various field strengths, and the maximum of the plot determines the nucleation barrier (ΔU_{nuc}^*) and the size of the critical nucleus (N^*) . For example, at $\varepsilon_{OP} = 1.0 \text{ V/nm}$, the nucleation barrier is $\approx 1.74 \times 10^5 k_B T$, indicating an extremely low nucleation probability at room temperatures even under a high electric field. The high 1D interfacial energy σ_i and the small magnitude of p_u together make it energetically challenging to switch a 2D domain in monolayer α -In₂Se₃. Under experimental conditions, the presence of defects could reduce the nucleation barrier by reducing σ_i .

Domain-Wall-Assisted Ferroelectric Switching. We will now demonstrate that pre-existing 1D domain walls can lower the switching field dramatically. When viewed from the out-of-plane direction of a single domain, the two layers of In atoms resemble the hexagonal lattice of monolayer *h*-BN with a (projected) bond length of *a*, while middle-layer Se atoms occupy only one type of lattice site (Figure 1b). There exist



Figure 4. Avalanche dynamics of 1D domain walls driven by ε_{OP} in 2D α -In₂Se₃. (a) Formation of 1D domain walls. The 180° walls separating P^+ and P^- domains can be created by an in-plane shift of a section of middle-layer Se atoms in either direction A or B by a distance of a, accompanied by an out-of-plane shift that flips the polarization. Type-A walls can be categorized as DW_{A,s} characterized by short Se–Se bonds at the wall and DW_{A,I} featuring large Se–Se separations. The green arrows denote the shift directions of Se atoms from their initial positions to the final positions. (b) Temporal evolution of the averaged position (x_{DW}) of DW_{A,s} driven by ε_{OP} obtained from MD simulations of a 4000-atom supercell. DW_{A,I} is immobile while DW_{A,s} moves abruptly and intermittently, indicating avalanche dynamics. The error bar scales with the geometrical roughness (global width) of the wall. The insets illustrate the flatness of DW_{A,s} in (c) evolves to a transient interface MA in (d) via $P^-@L_1 \rightarrow M@L_1$ and $P^-@L_2 \rightarrow A@L_2$. Immediately following that, two atomic movement patterns denoted as I and J in (d) are possible. The concerted occurrence of I and J results in fast sideway movement of MA in (f). The failure of movement J recovers the Miller-Weinreich line-by-line mechanism in (e). (g) Schematics of energy profiles for line-by-line mechanism (solid line) and stoneskipping-like mechanism (dashed line). The bursts of domain wall motions in (b) are attributed to the fast-moving MA interface and the periods of inactivity are due to the reactivation of DW_{A,s}.

four variants of 180° domain walls, grouped into two pairs (A and B), that can be generated by an in-plane shift of a section of middle-layer Se atoms along the direction connecting In atoms by a distance of *a* accompanied by an out-of-plane shift that flips the polarization direction. As illustrated in Figure 4a, for each pair, there is a wide domain wall characterized by long Se-Se separations (e.g., $DW_{A,l}$) and a narrow domain wall featuring short Se–Se bonds (e.g., $DW_{A,s}$). We focus on type-A walls for their greater thermodynamic stability compared to type-B walls (see Supplementary Section IX). Our MD simulations further show that only $DW_{A,s}$ is movable by ε_{OP} ; $DW_{A,l}$ is immobile, consistent with its large barrier of 0.7 eV for domain wall motion, as predicted by DFT-based NEB calculations (see Table S2 in Supporting Information). The temporal evolution of the averaged position of DW_{A,s} driven by $\varepsilon_{\rm OP}$ (Figure 4b) unveils two characteristics that differ distinctly from 2D domain walls in bulk ferroelectrics.^{43,44} First, the motion of $DW_{A,s}$ exhibits avalanche dynamics,⁴⁵ wherein this 1D interface moves abruptly and intermittently. The

distributions of the lifetimes of avalanche processes can be found in Supplementary Section X. Second, $DW_{A,s}$ acquires dynamic roughening: the initially flat wall becomes curved during its motion. The geometrical roughness, represented as error bars in Figure 4b, is characterized by a global width of ≈ 1.8 Å.

By analyzing MD trajectories with a fine time resolution down to femtoseconds, we identify a "stone skipping"-like mechanism that explains the two intrinsic features of $DW_{A,s}$ motion emerged in the absence of defects (disorder pinning). As depicted in Figure 4c, in the presence of ε_{OP} , a line of Se atoms (L_1) closest to the boundary move toward the bottom of nearby In^{up} atoms (denoted as $P^- @L_1 \rightarrow M@L_1$). Simultaneously, a line of In^{dn} atoms (L_2) shift toward those Se atoms of L_1 (denoted as $P^- @L_2 \rightarrow A@L_2$). This contrasts with the layer-by-layer switching mechanism pioneered by Miller and Weinreich for sideway motion of 2D domain walls.⁴⁶ Here, the movement of 1D DW_{As} engages two lines of atoms and is



Figure 5. Velocity of 1D domain walls driven by ε_{OP} in 2D α -In₂Se₃. Violin plot of domain wall velocity (ν) at (a) 300 K and (b) 400 K. The mean velocity $\overline{\nu}$ is fitted to eq 2 that describes a creep process. We find $\nu_0 = 247$ m/s and $\mu = 2$. (c) Plot of $\ln(\overline{\nu})$ versus $1/\varepsilon_{OP}^2$ curves for different temperatures. All linear fits (dashed lines) converge at the same intercept corresponding to $\nu_0 = 247$ m/s.

somewhat reminiscent of the hypothesized "nuclei stacking" that is assumed to occur in a high-field-induced mobile rough wall (though rarely observed).47 The transient interface, $M@L_1$ and $A@L_2$, can jointly serve as a moving front (Figure 4d). Specifically, subsequent processes of $A@L_2 \rightarrow M@L_2$ and $P^- (aL_3 \rightarrow A (aL_3, achieved via atomic movement pattern J)$ (Figure 4d), effectively move the MA interface sideways by a distance of a (Figure 4f). At steps where movement J does not take place, the line-by-line switching mechanism is recovered as the net outcome is $P^- @L_1 \rightarrow P^+ @L_1$ (Figure 4e). We propose that the MA interface is an "emergent" high-energy interface that only needs to overcome a small kinetic barrier to move (see the dashed line in Figure 4g), analogous to a swiftly skipping stone on water. The probabilistic failure of movement J could trigger the relaxation of MA to a flat, low-energy interface $(DW_{A,s})$, the movement of which must overcome a large barrier (see the solid line in Figure 4g). This stoneskipping-like mechanism intuitively explains the bursts of domain wall motions (attributable to the emergent fast-moving MA interface) separated by periods of inactivity (due to the reactivation of $DW_{A,s}$). The dynamic roughening of $DW_{A,st}$ manifested as a wavy moving font (see MD snapshots in Figure S18), is a consequence of the interplay between two distinct mechanisms of domain wall motion along an extended 1D interface. Across larger length scales, specific sections of the interface progress through the slower, line-by-line mechanism, while other segments advance more rapidly via the stoneskipping-like mechanism. This differential speed of movement along the interface's length results in the curvature during its motion. We note that during the period when the average position of the wall remains unchanged, the wall still exhibits significant dynamics: the interface fluctuates around the average position (see Figure S19). This behavior is indicative of a thermally driven activation process.

We use MD simulations to quantitatively estimate the velocity (v) of DW_{A,s} over a wide range of temperatures (T) and ε_{OP} . It is noted that the value of v is calculated by measuring the distance that the wall traverses within a specific time frame, while also taking into account the periods of

inactivity when the wall is stationary. Due to the inherent avalanche dynamics, the values of ν , obtained from multiple MD trajectories, exhibit a considerable fluctuation for a specific $\varepsilon_{\rm OP}$ and *T*, as shown by the violin plots at 300 and 400 K (Figure 5a,b). Even in the absence of defects, we discover that the mean 1D domain wall velocity, $\overline{\nu}$, can be well described with a creep process as^{48,49}

$$\overline{\nu} = \nu_0 \exp\left[-\left(\frac{\varepsilon_a}{\varepsilon}\right)^{\mu}\right] \tag{2}$$

where v_0 is the domain wall velocity under an infinite field, ε_a is the temperature-dependent activation field. Within a statistical description of domain wall motion as a critical phenomenon, that is, an elastic interface moving in random media, μ is the creep exponent that depends on the dimensionality of the interface and the universality class of the disorder landscape pinning the interface.²⁹ As depicted in Figure 5c, the plots of $\ln(v)$ versus $1/\varepsilon_{OP}^2$ curves yield linear relationships across a broad spectrum of field strengths (1.0-2.8 V/nm) and various temperatures (300-400 K). Notably, all linear fits converge at the same intercept that corresponds to $v_0 = 247$ m/s. This serves as a strong evidence for a creep exponent, $\mu = 2$, higher than the well-known value of μ = 0.25 for 1D magnetic domain walls in ultrathin magnetic films²⁹ as well as $\mu = 1$ for 2D ferroelectric domain walls in typical perovskite ferroelectrics.^{43,50} We propose $\varepsilon_{\mathrm{OP}}$ -driven creep motion of $\mathrm{DW}_{A,s}$ in monolayer α -In₂Se₃ probably belongs to an entirely unreported universality class. A higher value of creep exponent implies that this interface is more sensitive to changes in the magnitude of $\varepsilon_{\mathrm{OP}}$, especially at low driving forces, which is advantageous for fine-tuning domain wall mobility. Moreover, we observe the absence of an intrinsic creep-depinning transition, even at a colossal field strength of 2.8 V/nm (28 MV/cm), likely attributable to the small Born effect charges (0.49 for In and -0.45 for Se) in the out-of-plane direction: the weak $\varepsilon_{\rm OP} - P_{\rm OP}$ coupling is insufficient to reduce the barrier of domain wall motion compared to thermal fluctuations, thus leading to persistent creep behavior of $DW_{A,s}$.



Figure 6. Dynamics of 1D domain walls driven by $\varepsilon_{\rm IP}$ in 2D α -In₂Se₃. Temporal progression of DW_{A,s} in the presence of $\varepsilon_{\rm IP}$ applied (a) parallel to the wall ($\varepsilon_{\rm IP}||\text{DW}$) and (b) perpendicular to the wall ($\varepsilon_{\rm IP}\perp$ DW), revealing avalanche dynamics in both cases. The field strength is 0.1 V/nm. (c) Violin plot of domain wall velocity as a function of the relative orientation (θ) between $\varepsilon_{\rm IP}$ and the wall at 360 K. (d) *T*- and $\varepsilon_{\rm IP}$ -dependent mean velocity of DW_{A,s} for $\theta = 45^{\circ}$. The velocity data at temperatures above 340 K and $\varepsilon_{\rm IP} \ge 0.06$ V/nm demonstrate depinning characteristics and is fitted to eq 3. We find $\varepsilon_{\rm IP}^{\rm C0} = 0.056$ V/nm and $\Theta = 0.736$ (bold gray line). Velocity data within the lower temperature range (300–340 K) and lower field range (0.06–0.12 V/nm) show creep behavior. The linear relationship (dashed lines) between $\ln(\bar{\nu})$ and $1/\varepsilon_{\rm IP}^2$, as shown in the inset, confirms a creep exponent of $\mu = 2$. The linear fits also converge at the same intercept that corresponds to $\nu_0 = 247$ m/s.

Domain Wall Motion Driven by In-Plane Electric **Fields.** The movement of $DW_{A,s}$ driven by ε_{OP} involves inplane displacements of In and Se atoms near the boundary (Figure 4c-f), hinting at a potential coupling between DW_{As} and in-plane fields. Considering the symmetry, the presence of $\text{DW}_{\text{A},\text{s}}$ locally disrupts the C_{3v} point group symmetry, in turn generating local dipoles in DW_{As} that could be coupled to $\varepsilon_{\rm IP}$. This is confirmed by our finite-field MD simulations, which demonstrate ε_{IP} -driven DW_{A,s} motion. This phenomenon is analogous to the ferroelectric domain walls investigated by Lu Guangming et al., where the bulk is nonpolar but the domain walls exhibit polarization.⁵¹ It was found that the polarization hysteresis results from the nucleation of interfaces near surfaces, followed by the evolution of the domain pattern. Moreover, monolayer α -In₂Se₃ with movable domain walls resembles the Bloch-line ferroelectrics featuring polar domain walls in paraelectric materials, as proposed by Salje and Scott.⁵² Owing to the large in-plane Born effective charges of Se and In atoms, applying $\varepsilon_{\mathrm{IP}}$ of 0.12 V/nm is sufficient to drive the movement of $DW_{A,s}$ within 100 ps at 300 K. This field strength is notably lower than what would be needed when $\varepsilon_{\mathrm{OP}}$ is applied, and is comparable to the field strengths (\approx 0.2 V/nm) used in experiments.²

The ε_{IP} -driven DW_{A,s} motion is found to exhibit a pronounced field-orientation dependence. When ε_{IP} is applied parallel to DW_{A,s} (ε_{IP} |IDW), this 1D interface shows an equal likelihood of moving either to the left or the right, corresponding microscopically to the equally probable hopping processes of Se atoms situated in proximity to DW_{A,s} (Figure 6a). This behavior is a manifestation of spontaneous symmetry

breaking: while $\varepsilon_{\mathrm{IP}}$ does not inherently favor any particular direction due to the lack of physical in-plane polarization, the wall opts for a specific direction, which is induced by thermal activation. The temporal progression of the domain wall position (Figure 6a) clearly demonstrates that $DW_{A,s}$ retains the avalanche dynamics and oscillates back and forth in a stochastic manner in the case of $\varepsilon_{\rm IP}$ ||DW. In comparison, when $\varepsilon_{\rm IP}$ is applied perpendicular to DW_{A,s} ($E_{\rm IP} \perp$ DW), the wall moves deterministically, in the direction counter to that of the Se atom hopping (Figure 6b). We map out \overline{v} as a function of the relative orientation (θ) between ε_{IP} (of 0.1 V/nm) and the wall at 360 K, showing a strong anisotropy with the maximum velocity peaking at $\theta \approx 45^{\circ}$ (Figure 6c). Such highly tunable domain wall mobility in 2D ferroelectrics is beneficial for the controlled design of polarization switching speed and domain wall memory.⁵² This also highlights domain wall dynamics at reduced dimensions, as demonstrated in a recent experimental study that shows as sample thickness decreases, domain walls exhibit increased curvature and density due to dominant dipole-dipole interactions.53

The *T*- and $\varepsilon_{\rm IP}$ -dependent mean velocity of DW_{*A,s*} for θ = 45° is displayed in Figure 6d, indicating an intrinsic creepdepinning transition.⁴³ In particular, the velocity data at temperatures exceeding 340 K overlap when $\varepsilon_{\rm IP} > 0.06$ V/nm, a hallmark feature of depinning wherein the velocity becomes temperature independent. These velocity data can be fitted to

$$\overline{\nu} \propto (\varepsilon_{\rm IP} - \varepsilon_{\rm IP}^{\rm C0})^{\Theta} \tag{3}$$

where Θ is a velocity exponent and $\varepsilon_{\rm IP}^{\rm C0}$ is the crossing field at zero Kelvin. The fitting yields $\Theta = 0.736$, a value nearly identical to the reported velocity exponent of 0.72 for 90° domain walls in PbTiO₃. This implies the existence of universal depinning dynamics for domain walls in 2D and 3D ferroelectrics. At temperatures of 340 K or lower, the velocity has a strong dependence on temperature and exhibits a nonlinear relationship with $\varepsilon_{\rm IP}$, suggesting a creep behavior. As presented in the inset of Figure 6d, the velocity data in the creep region can be well described by eq 2 using the same parameters, $v_0 = 247$ m/s and $\mu = 2$, as derived from $\varepsilon_{\rm OP}$ -driven DW_{A,s} motions shown in Figure 5c. The velocity data collected under both $\varepsilon_{\rm IP}$ and $\varepsilon_{\rm OP}$ affirm the robustness of an atypical creep exponent of 2, supporting the presence of a unreported universality class.

CONCLUSIONS

Our investigation, which integrates both experimental characterizations and theoretical simulations on the ferroelectric switching in 2D α -In₂Se₃, addresses the three aforementioned questions. First, PFM studies following rigorous protocols yield conclusive evidence indicating the absence of measurable $P_{\rm IP}$ in α -In₂Se₃. Specifically, the comparative study of angle-resolved IP-PFM on both α -In₂Se₃ and NbOI₂ demonstrates that the measured lateral response in α -In₂Se₃ does not originate from intrinsic in-plane piezoresponse, but is due to a crosstalk artifact from the out-of-plane signal.

Second, the forbidden splitting of Wyckoff orbits for the transition from paraelectric β -In₂Se₃ to ferroelectric α -In₂Se₃ introduces a trade-off between the robustness of $P_{\rm OP}$ and the difficulty in switching it: the lack of a symmetry-adapted polar mode renders P_{OP} stable against the depolarization field but also makes $\varepsilon_{\rm OP}$ - $P_{\rm OP}$ coupling rather inefficient. This splitting restriction principle, along with the resultant difficulty of ε_{OP} driven polarization reversal, is expected to be a prevalent characteristic across a wide spectrum of vdW bilayers exhibiting sliding ferroelectricity and morié ferroelectricity. The existence of domain walls, particularly $DW_{A,s}$ is found to be essential for the ferroelectric switching driven by ε_{OP} in 2D α -In₂Se₃. The giant magnitude of ε_{OP} (at the order of 1 V/nm) required for moving domain walls, as predicted by our MD simulations and corroborated by experiments,⁴ can be attributed to the weak $\varepsilon_{\rm OP}$ - $P_{\rm OP}$ coupling.

Despite the lack of switchable $P_{\rm IP}$ in a single-domain monolayer, the presence of DW_{A,s} breaks the out-of-plane 3fold rotational symmetry on a local level, allowing for a coupling between local dipoles of DW_{A,s} and $\varepsilon_{\rm IP}$. Benefiting from the large in-plane Born effective charges and the mechanism of DW_{A,s} motion involving in-plane atomic displacements, applying $\varepsilon_{\rm IP}$ proves to be more efficient than using $\varepsilon_{\rm OP}$ for inducing ferroelectric switching, resolving a longstanding inconsistency between experimental observations and theoretical predictions.

We can also narrate our findings in the context of the modern theory of polarization.⁵⁴ The polarization calculated by the Berry phase method is termed *formal polarization*, which is a lattice-valued property and needs only be invariant modulo a polarization quanta under point-group operations. This means the formal polarization can be nonzero in structures with 4-fold or 3-fold rotational symmetry, such as perovskite LaAlO₃⁵⁵ and monolayer MoS₂.⁵⁶ The formal polarization can

have physical consequences. For example, the discontinuity of the formal polarization at the edges of MoS_2 nanoribbons leads to metallic states.⁵⁶ Therefore, α -In₂Se₃, similar to MoS_2 with 3-fold rotational symmetry, should exhibit in-plane formal polarization.

However, it is well established that the experimental value of the spontaneous polarization obtained from the polarizationelectric field hysteresis loops should correspond to the effective polarization, which is the change in the formal polarization along the switching pathway. Our MD simulations revealed that applying an in-plane electric field to a single-domain monolayer α -In₂Se₃ actually drives an irreversible $\alpha \rightarrow \beta'$ phase transition rather than the ferroelectric switching. For this reason, we state that single-domain monolayer α -In₂Se₃ does *not* have reversible in-plane effective polarization.

Interestingly, the presence of a domain wall breaks the 3-fold rotational symmetry locally, and the discontinuity of the formal polarization causes the wall to acquire localized polarization charge. This is consistent with reports of localized polarization charges at edges or boundaries in monolayer MoS_2 nanoribbons.⁵⁶ Therefore, the motion of domain walls driven by an inplane electric field can be heuristically understood as the electrostatically driven motion of a charged interface. This process could produce switching current in a hysteresis loop measurement as well. In this sense, it is appropriate to conclude that monolayer α -In₂Se₃ with domain walls could exhibit in-plane effective polarization.

Finally, the 1D ferroelectric domain wall exhibits avalanche dynamics when subjected to electric fields, stemming from a competition between two distinct domain wall motion mechanisms: the conventional Miller-Weinreich line-by-line mechanism and the stone-skipping-like mechanism facilitated by an emergent high-energy interface. Our extensive data set of domain wall velocity at various temperatures and field strengths (including both $\varepsilon_{\rm OP}$ and $\varepsilon_{\rm IP}$) reveals a creep exponent of $\mu = 2$, diverging from the known values for magnetic domain walls²⁹ and ferroelectric domain walls in bulk perovskite ferroelectrics.^{43,50}

Creep motion of a *d*-dimensional elastic interface moving in a d + 1-dimensional random media is a physical behavior presented in a vast range of diverse systems such as vortices in type-II superconductors,⁵⁷ density waves,⁵⁸ burning⁵⁹ and wetting fonts,⁶⁰ and cell migration.⁶¹ The indication of an entirely unreported universality class associated with $\mu = 2$, as reported here, highlights the potential of 1D ferroelectric domain walls in 2D ferroelectrics for in-depth understanding of the fundamental physics of moving interfaces in reduced dimensions. Furthermore, the strong anisotropic response of domain walls to external fields and tunable onset field for the creep-depinning transition can be harnessed to configure the switching speed in 2D α -In₂Se₃. Given the structural similarity between monolayer α -In₂Se₃ and vdW bilayers with sliding ferroelectricity, we anticipate the atomic-level insights and quantitative understanding of domain wall mobility presented here will contribute to the comprehension of intrinsic ferroelectric switching in a broad range of 2D ferroelectrics, ultimately leading to enhanced functionalities of 2D ferroelectric-based devices.

METHODS

DFT Calculations. All first-principles density functional theory calculations are performed using the Vienna ab initio Simulation Package (VASP).^{62,63} The interaction between core ions and

electrons is modeled using the projector augmented wave (PAW) method.⁶⁴ We choose the PBE functional as the exchange-correlation functional,⁶⁵ and the van der Waals (vdW) interaction is considered using the Grimme method with a zero-damping function.⁶⁶ A slab model incorporating a vacuum layer with a thickness exceeding 20 Å along the z-axis is used to model monolayer In₂Se₃; the dipole correction is employed to counteract spurious interactions between periodic images across the vacuum layer. DFT calculations are based on an energy cutoff of 700 eV, a $7 \times 7 \times 1$ Monkhorst–Pack k-point mesh for Brillouin zone sampling of the unit cell, and an energy convergence threshold of 10^{-8} eV for electronic self-consistency. The convergence criterion for structure optimization is set to 10^{-7} eV in energy. An external electric field is modeled by introducing a planar dipole layer at the center of the vacuum region.⁶⁷ The climbing image nudged elastic band (CL-NEB) method⁶⁸ with force convergence set to 0.01 eV/Å is used to determine the minimum energy path for polarization reversal.

Force Field of 2D α -ln₂Se₃. The force field utilized in our largescale molecular dynamics simulations is a deep neural network-based model potential, known as deep potential (DP). 69,70 The DP model maps an atom's local environment to its energy (E_i) , where the total energy E is obtained as $E = \sum_{i} E_{i}$. We have successfully trained a DP model of monolayer $\mathrm{In}_2\mathrm{Se}_3$ using a concurrent learning process that effectively updates the first-principles-based training database.⁴² The neural network architecture consists of three hidden layers, with each layer containing 240 neurons. The final training database comprises 22,600 monolayer configurations and 2163 bulk structures. With 10⁶ learnable parameters, the model has demonstrated accuracy in fitting to DFT energies and atomic forces (Figure S9). For the atomic forces of all atoms in the entire training database, the mean absolute error (MAE) and root mean squared error (RMSE) are 0.068 and 0.096 eV/Å, respectively. The model potential is capable of predicting a variety of thermodynamic properties of In₂Se₃ polymorphs (including α , β , and β'), the DFT potential energy surface for the in-plane sliding of the central Se sublayer, temperature-driven phase transitions, and energy profiles for polarization reversal and 180° domain wall motions in monolayer α -In₂Se₃ (Figure S10). We note that all local atomic environments involved in domain wall motions are well-represented in the training database (Figure S11).

Molecular Dynamics. We perform constant-temperature constant-volume (NVT) deep potential molecular dynamics simulations using LAMMPS.⁷¹ The temperature is maintained using the Nosé-Hoover thermostat and the time step is set to 1 fs. The free-standing monolayer α -In₂Se₃ containing type-A domain walls is modeled using a $20 \times 40 \times 1$ supercell comprised of 4000 atoms and a vacuum layer of 22 Å under periodic boundary conditions, as shown in Figure S17. The effects of electric fields are modeled in classical MD simulations through the force method.⁷² This approach involves adding an additional force to each ion, calculated as the product of the ion's Born effective charge and the magnitude of the electric field. We note that at finite temperatures, the unstained free-standing monolayer α - In_2Se_3 can spontaneously transition into β' - In_2Se_3 due to their close thermodynamic stability, especially in the presence of domain walls and/or external in-plane electric fields. This is actually consistent with several experimental observations that the phase transition from α - In_2Se_3 to β' - In_2Se_3 can be induced by strain.^{10,12} To explore the intrinsic switching dynamics of 1D domain walls in monolayer α -In₂Se₃, we imposed a minor tensile strain (\approx 1.6%) to stabilize the α phase and the domain walls. At a specific temperature, an equilibrium run lasting at least 1 ns is executed before the electric field is introduced to initiate domain wall movement and to measure the velocity (v) of the domain wall. The value of v is determined directly by tracking the distance traveled by the wall within a specific time frame, while also taking into account the periods of inactivity when the wall is stationary to capture the effect of avalanche dynamics. We carry out 20 independent runs (ranging from 0.1 to 1 ns) for specific temperature and electric field strength to obtain the velocity distribution of the domain wall. The methodology for determining the domain wall position during its motion relies on the coordination numbers of Se atoms. At a specific time point t (in picosecond), we

first determine the averaged structure by averaging configurations sampled every 0.1 ps within a time interval from $t - \delta$ to t, where $\delta = 1-5$ ps depending on the domain wall speed. This treatment reduces the thermal noise. We then search for the Se–In coordination within a radius of 4.2 Å centered around the Se atom. If the coordination number of a Se atom exceeds 4, we record its position, and these Se atoms define the position of the domain wall. In an effort to improve reproducibility, we have made our training database, force field model, training metadata, essential input and output files publicly available in an open repository.⁷³

Piezoresponse Force Microscopy. The PFM studies are conducted using a commercial atomic force microscope (Oxford Instrument, MFP-3D origin+). DART method is employed for PFM imaging and local switching spectroscopy measurements. Two types of conductive AFM probes with spring constants of ≈ 2.8 N/m (Asylum Research, ASYELEC.01-R2) and ≈ 0.2 N/m (Nanoworld, CONTPt) are used for cross validation and comparison. Micro-Raman spectroscopy and mapping are measured by an integrated confocal Raman microscope (Horiba, Xplora Plus) using a 532 nm laser focused by 50X long working distance objective.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsnano.4c06619.

Comparison between dipole locking mechanism and splitting restriction principle; phase transitions during a heating—cooling cycle; previous PFM studies; Raman and SHG measurements; estimation of out-of-plane switching fields; accuracy of the DP model used in MD; sliding ferroelectricity; critical nucleus; energetics of domain walls; lifetimes of avalanche processes; dynamic walls during the stationary period; and dynamic walls during the stationary period (PDF)

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Notes

The authors declare no competing financial interest.

ACKNOWLEDGMENTS

L.B., C.K., T.Z., and S.L. acknowledge the supports from National Natural Science Foundation of China (12304128, 52002335) and Westlake Education Foundation. The computational resource is provided by Westlake HPC Center. We thank the Research Center for Industries of the Future (RCIF) at Westlake University for partially supporting this work. We also thank Dr. Jiawei Huang for useful discussions regarding the categorization of domain walls. L.Y. acknowledges the supports from National Natural Science Foundation of China (No. 12074278) and Suzhou Science and Technology Bureau (ZXL2022514).

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